

--	--	--	--	--	--	--	--	--	--

***B.Tech. Degree II Semester Regular/Supplementary Examination in
Marine Engineering June 2024***

**19-208-0201 ENGINEERING MATHEMATICS II
(2019 Scheme)**

Time: 3 Hours

Maximum Marks: 60

Course Outcome

On successful completion of the course, the students will be able to:

- CO1: Solve linear system of equations and to determine eigen values and vectors of a matrix.
 CO2: Solve ordinary differential equations and linear differential equations of higher orders with constant coefficient and apply them in engineering problems.
 CO3: Determine fourier series expansions of functions and transforms.
 CO4: Solve linear differential equations and Integral equations using Laplace transforms.
 CO5: Understand the basic concepts of probability and different probability distributions.

Bloom's Taxonomy Levels (BL): L1 – Remember, L2 – Understand, L3 – Apply, L4 –Analyze, L5 – Evaluate,
 L6 – Create

PI – Programme Indicators

(Answer *ALL* questions)

(5 × 15 = 75)

		Marks	BL	CO	PI
I. (a) Find the Eigen values and Eigen vectors of the matrix.	7	7	L3	1	1
$\begin{bmatrix} 1 & 0 & -1 \\ 1 & 2 & 1 \\ 2 & 2 & 3 \end{bmatrix}$					
(b) By reducing to Echelon form find the rank of the matrix.	8	8	L3	1	1
$\begin{bmatrix} 1 & 0 & 2 & 1 \\ 0 & 1 & -2 & 1 \\ 1 & -1 & 4 & 0 \\ -2 & 2 & 8 & 0 \end{bmatrix}$					
OR					
II. (a) Verify Cayley Hamilton Theorem for the matrix	8	8	L3	1	1
$A = \begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix}$ and find its Inverse.					
(b) Using Jacobi's iteration method, solve the following by taking six iterations.	7	7	L3	2	1
$20x + y - 2z = 17$ $3x + 20y - z = -18$ $2x - 3y + 20z = 25$					

(P.T.O.)

BT MRE-II(R/S)-06-24-3233

	Marks	BL	CO	PI														
III. (a) Solve $(x+1)\frac{dy}{dx} - y = e^{3x}(x+1)^2$.	7	L3	2	1														
(b) Solve $\frac{d^2y}{dx^2} - 3\frac{dy}{dx} + y = \sin 2x + e^{5x}$.	8	L2	2	1														
OR																		
IV. Solve the simultaneous equations, $\frac{dx}{dt} + 2x - 3y = 0$ $\frac{dy}{dt} - 3x + 2y = 0$.	15	L3	2	1														
V. (a) Find the Fourier series expansion of $f(x) = x, -\pi \leq x \leq \pi$.	8	L3	2	1														
(b) Find the half range cosine series expansion of $f(x) = x^2, 0 \leq x \leq \pi$.	7	L3	2	1														
OR																		
VI. (a) Prove that $\beta(m, n) = \frac{\Gamma(m)\Gamma(n)}{\Gamma(m+n)}$.	7	L3	3	1														
(b) Find the Fourier series expansion of $f(x) = x^2, -\pi \leq x \leq \pi$.	8	L3	3	1														
VII. (a) Use transform methods to solve $\frac{d^2x}{dt^2} - 2\frac{dx}{dt} + x = e^t$ with $x(0) = 2$ and $x'(0) = -1$.	8	L3	4	1														
(b) Find the Laplace transform of $e^{-3t}(2 \cos 5t - 3 \sin 5t)$.	7	L3	4	1														
OR																		
VIII. (a) Apply Convolution theorem to evaluate $L^{-1}\left[\frac{s}{(s^2 + a^2)^2}\right]$.	8	L2	4	1														
(b) Find the inverse Laplace transform of $\frac{s^2 - 3s + 4}{s^3}$.	7	L3	4	1														
IX. A random variable X has the following probability distribution.	15	L3	5	1														
	<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>X</th> <th>-2</th> <th>-1</th> <th>0</th> <th>1</th> <th>2</th> <th>3</th> </tr> </thead> <tbody> <tr> <td>P(X=x)</td> <td>$\frac{1}{10}$</td> <td>k</td> <td>$\frac{1}{5}$</td> <td>2k</td> <td>$\frac{3}{10}$</td> <td>3k</td> </tr> </tbody> </table>				X	-2	-1	0	1	2	3	P(X=x)	$\frac{1}{10}$	k	$\frac{1}{5}$	2k	$\frac{3}{10}$	3k
X	-2	-1	0	1	2	3												
P(X=x)	$\frac{1}{10}$	k	$\frac{1}{5}$	2k	$\frac{3}{10}$	3k												
(i) Find the value of k																		
(ii) Find $P(-2 < X < 2)$																		
(iii) Find $P(X < 2)$.																		
OR																		
X. (a) The mean and variance of a binomial random variable X are 16 and 8 respectively. Find $P(X = 0)$.	7	L5	5	1														
(b) Ten coins are thrown simultaneously. Find the probability of getting at least 7 heads.	8	L5	5	1														

Blooms's Taxonomy Level

L2 - 15%, L3 - 75%, L5 - 10%.